#### Illinois Alternate Assessment Mathematics Frameworks Priorities Grade 11

In the spring of 2006, a team of Illinois educators created the new Illinois Alternate Assessment (IAA) Frameworks. The purpose of the frameworks is to prioritize the skills and knowledge from the Illinois Learning Standards for students with the most significant cognitive disabilities, in order to develop a new Illinois Alternate Assessment. The Illinois State Board of Education (ISBE) contracted Pearson Educational Measurement (PEM), and their subcontractor partners, Beck Evaluation and Testing Associates, Inc. (BETA), and the Inclusive Large Scale Standards and Assessment (ILSSA) group, to develop the new IAA in grades three through eight and 11 for Reading and Mathematics; in grades four, seven, and 11 for Science; and in grades three, five, six, eight, and 11 for Writing. BETA's responsibilities include providing event-based assessment activities linked to the IAA Frameworks, developing the assessment rubric, and incorporating principles of Universal Design for Learning. ILSSA's responsibilities include facilitating the development of the IAA Frameworks and providing statewide staff development on how to access grade-level curriculum. Pearson Learning Group (PLG) is a division of PEM and their responsibilities include providing a customized online scoring tool along with training to use this feature.

During the framework development meetings, educators were divided into development teams based on both content area and grade level focus. Addressing reading, writing, mathematics, mathematics, and science, each content area had one development team for elementary school, one for middle school, and one for high school. Each team consisted of at least one general education teacher, one special education teacher, and one content expert. The process used by the development teams to create the Illinois Alternate Assessment Frameworks was as follows:

The development teams reviewed each of the assessment objectives (statements coded with numbers such as 6.11.01) in grades three through eight. For each assessment objective, the teams:

- Identified the critical function, or the main idea of the objective;
- Wrote an instructional activity that could be used to teach the skills needed to meet the assessment objective in the general education classroom;
- Wrote a modified instructional activity that could be used to teach students with the most significant cognitive disabilities the same skills; and
- Identified three assessment activities that could be used to assess students with the most significant cognitive disabilities on the skills described in the modified activity.

After the development teams examined the assessment objectives and wrote both instructional and assessment activities for each grade level, the teams prioritized the assessment objectives and selected the assessment objectives which are most suitable for students with the most significant cognitive disabilities. The leadership team at ISBE reviewed these priorities for further refinement. These pilot priorities will form the basis for the new IAA performance test items. Following the completion of the fall 2006 writing pilot, a review may be necessary in order to determine if the new IAA priorities are appropriate and provide a comparable assessment to the general statewide assessment.

Using grade-level curriculum as the focus, the development teams described the instructional and assessment supports, accommodations, and assistive technology required to ensure access to quality instruction. The descriptions produced by the development teams were summarized into a set of statements designed to provide consistency across the content frameworks. These statements are as follows:

- Appropriate instruction must occur prior to the assessment activity.
- All activities must provide appropriate support, accommodations, and/or assistive technology during both the instructional activities and the assessment process. This may include the following:
  - The use of prompting strategies, ranging from minimum prompts to full physical assistance in order to create a learning continuum for correct responses.
  - The use of assistive technology, ranging from low tech to high tech.
  - The reduction of breadth, depth, and/or complexity.
- Specific instructional strategies and the instructional environment for the individual student vary and should be determined by the student's IEP team.
- During assessment activities, the students should use the mode of communication that they used to learn and practice the skills during instructional activities.
- Instruction should be presented to the student in a way that is authentic, accessible, and meaningful (e.g., tactile objects, picture symbols, or use of a text reader), to ensure the student has multiple opportunities to learn and demonstrate knowledge.

• Instruction should take place within the context of grade-level content, using age-appropriate activities and materials, regardless of the placement of the student.

IAA Mathematics Priorities Grade 11-November 14, 2006

#### Illinois Alternate Assessment Mathematics Frameworks Priorities Grade 11

• Instruction must incorporate age-appropriate activities and materials which represent the same grade level content as their peers without disabilities. However, the activities and materials may be adapted to meet the individual needs of the student (e.g., reduce the language requirements or difficulty of the task) as long as the context of the materials used by same age peers remains intact.

All instructional practices should occur using available resources and materials familiar to the learners.

Communication skills are essential to the assessment of students with significant cognitive disabilities. Symbolic communication skills form the foundation for reading, mathematics, and writing. Students with significant cognitive disabilities are very diverse in their communication ability. Some students communicate symbolically, while others communicate in highly individualized ways. There are some important considerations in the development of symbolic communication skills which include the following:

- All students communicate regardless of their level of symbolic language use.
- Students with the most significant cognitive disabilities can acquire generalized use of objects (or object selection) to communicate preferences (Hetzroni, Rubin, Konkol, 2002).
- Language learners must use symbols repeatedly, interactively, and generatively during meaningful and ongoing activities in language-rich environments (Goossens, Crain, & Elder, 1992; Cafiero, 1998; Goossens, et al., 1992; Romiski & Sevcik, 1996; Miller & Eller-Miller, 2002; Mirenda, 2003).
- Competent use of language for multiple purposes, audiences, and contexts facilitate the metalinguistic skills required for reading comprehension (Rankin, Harwood, & Mirenda, 1994). The assessment activities in this document reflect three types of students who represent the continuum of communication skills within this student population.
  - The first activity is designed for students who inconsistently respond to communication and inconsistently use words, objects, or gestures to communicate expressively.
  - The second activity is for learners who are beginning to use understandable communication through gestures, pictures, objects/textures, points, etc., to clearly express a variety of intentions.
  - The third activity is for students who are using verbal or written words, sign language, Braille, or any language-based augmentative system to request, initiate, and respond to questions, describe things or events, and express refusal.

Throughout the frameworks document, the suggested general education instructional and modified instructional activities are written in plural form, as instruction is typically provided to a whole class. However, the instruction for these activities may be provided in the context of whole class instruction, small group instruction, or individually based on student needs. Conversely, the assessment activities are written in the singular form, as the IAA is a standard assessment measuring individual performance.

The process of reviewing the frameworks and aligning the new IAA to the Illinois Learning Standards and regular assessment is an ongoing process. The activities in this document were created by Illinois teachers and are only suggested activities that may be used to teach the assessment objectives listed. The activities, materials, and techniques listed in the frameworks are just one possible way to teach these assessment objectives and should not to be considered the state-mandated strategy for teaching any given assessment objective. Teachers should feel comfortable in using other strategies, materials, or activities that may already be in place or familiar to the teacher. The IAA Frameworks and the IAA itself will continue to be reviewed and adjusted as changes occur with the Illinois Standards and/or the general assessment.

#### Illinois Alternate Assessment Mathematics Frameworks Priorities Grade 11

#### **State Goal 6: Number Sense**

#### **Representations and Ordering (Standard 6A)**

6.11.01 Recognize, represent, order, compare real numbers, and locate real numbers on a number line (e.g.,  $\pi$ ,  $\sqrt{2}$ ,  $\sqrt{5}$ , 2/3, -1.6).

## Computation, Operations, Estimation, and Properties (Standards B and C)

6.11.09 Solve problems involving estimates or data (e.g., use averages to estimate the cost of a job that includes labor and materials).

6.11.10 Perform numerical computations with real numbers.

6.11.13 Set up, evaluate, or solve single- and multi-step number sentences and word problems with rational numbers using the four basic operations.

## Ratios, Proportions, and Percents (Standard D)

6.11.18 Set up, evaluate, or solve common problems involving percent (e.g., sales tax, tip, interest, discount, markup, commission, compound interest).

#### **State Goal 7: Measurement**

#### Units, Tools, Estimation, and Application (Standards A, B, and C)

7.11.01 Change from one unit to another within the same system of measurement, including calculations with mixed units (e.g., 3 <sup>1</sup>/<sub>2</sub> hours plus 4 hours and 20 minutes; 2<sup>1</sup>/<sub>2</sub> feet minus 16 inches).

7.11.03 Determine and calculate to an indicated precision the length, width, height, perimeter/circumference, area, volume, surface area, angle measures, or sums of angle measures of common geometric figures or combinations of common geometric figures.

#### State Goal 8: Algebra

#### Representations, Patterns, and Expression (Standard A)

8.11.04 Determine a specific term, a finite sum, or a rule that generates terms of a pattern.

#### Connections Using Tables, Graphs, and Symbols (Standard B):

8.11.12 Create and connect representations that are tabular, graphic, numeric, and symbolic from a set of data.

#### **State Goal 9: Geometry**

## Properties of Single Figures and Coordinate Geometry (Standard A)

9.11.02 Identify and represent transformations (rotations, reflections, translations) of an object in the plane, and describe the effects of transformations on points in words or coordinates.

9.11.06 Identify a three-dimensional object from different perspectives.

9.11.07 Identify the relationship between two-dimensional patterns (e.g., nets) and related three-dimensional objects (e.g., cylinders, prisms, cones).

## State Goal 10: Data Analysis, Statistics, and Probability

#### Data Analysis and Statistics (Standards A and B)

10.11.01 Read, interpret, predict, interpolate, extrapolate, and use information from a variety of graphs, charts, and tables.

## Representations and Ordering (Standard A)

# 6.11.01 Recognize, represent, order, compare real numbers, and locate real numbers on a number line (e.g., $\pi$ , $\sqrt{2}$ , $\sqrt{5}$ , 2/3, -1.6).

Critical Eurotion	Suggested Conorol	Suggested Modified	Paggibla Aggagement Activity 1	Possible Assessment Activity 2	Possible Assessment Activity 3
Citical Function		Suggested Modified	rossible Assessment Activity I	rossible Assessment Activity 2	rossible Assessment Activity 5
	Education Activity	Instructional Activity			
Recognize, represent, order,	The teacher will	The teacher will	Given a number line, the	Given a number line and a	Given a number line, the
compare real numbers, and	demonstrate, explain and	demonstrate, explain, and	student will communicate	number, the student will identify	student will identify the
locate real numbers on a	compare the order of real	compare the order of real	understanding of number	the number and show its	number and write the number
number line (e.g., $\pi$ , $\sqrt{2}$ ,	numbers. Given 10 real	numbers. Given two	placement.	placement.	on the number line in the
$\sqrt{5}, 2/3, -1.6$ ).	numbers, the students	whole numbers (subset of			proper order.
	will place them on a	real numbers) plotted and			
	number line.	labeled on a number line,			
		the students will place a			
	Examples:	third number on the			
	Read numbers on a	number line.			
	number line.				
	Place numbers on the				
	number line.				
	Put numbers in order				
	from least to greatest or				
	greatest to least.				
	Compare numbers to				
	determine less than,				
	greater than or equal.				
	Place a dot on the				
	number line where a				
	certain number belongs.				

#### **Computation, Operations, Estimation, and Properties (Standards B and C)**

#### 6.11.09 Solve problems involving estimates or data (e.g., use averages to estimate the cost of a job that includes labor and materials).

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Critical Function	Suggested General	Suggested Modified	Possible Assessment Activity 1	Possible Assessment Activity 2	Possible Assessment Activity 3
	Education Activity	Instructional Activity			
Solve problems involving	The teacher will review	The teacher will review	Given a set of data, the student	Given a set of data, the student	Given a set of data, the student
estimates or data.	rules for rounding up or	rules for rounding up or	will indicate if the answer	will indicate from a set of answers	will determine the correct
	down and will model	down and will model	provided is correct.	which is correct.	answer.
	how to solve problems	how to solve problems			
	using estimation. The	using estimation. The		(e.g., Given a selection for a	(e.g., The student wants to buy
	students will solve a	students will be		vending machine item, the student	x, y, and z. How much money
	problem (e.g., A	instructed to choose 3		will estimate the number of dollars	will the student need?)
	notebook costs \$2.98.	grocery items. The		needed for a purchase.)	
	Approximately how	students will use			
	much would 4 notebooks	rounding up to the next			
	cost?).	dollar skill to estimate			
	-	what the total cost will be			
		for all three items.			

#### Computation, Operations, Estimation, and Properties (Standards B and C)

# 6.11.10 Perform numerical computations with real numbers.

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Critical Function	Suggested General	Suggested Modified	Possible Assessment Activity 1	Possible Assessment Activity 2	Possible Assessment Activity 3
	Education Activity	Instructional Activity			
Perform numerical	The teacher will review	The teacher will review	Given a temperature of three	Given a temperature of three	Given a temperature of three
computations with real	how to perform	how to perform	degrees below zero and a rise	degrees below zero and a rise in	degrees below zero and a rise
numbers.	numerical computations.	numerical computations.	in temperature of 10 degrees,	temperature of 10 degrees, the	in temperature of 10 degrees,
	The students will add	Using manipulatives, a	the student will provide the	student will provide the current	the student will provide the
	positive and negative	calculator, and/or a	current temperature from a	temperature from a choice of listed	current temperature.
	numbers with and	number line, the students	choice of two.	possible temperatures.	
	without a number line.	will perform addition,			
		subtraction,			
		multiplication, and			
		division problems.			

#### **Computation, Operations, Estimation, and Properties (Standards B and C)**

#### 6.11.13 Set up, evaluate, or solve single- and multi-step number sentences and word problems with rational numbers using the four basic operations.

Critical Function	Suggested General	Suggested Modified	Possible Assessment Activity 1	Possible Assessment Activity 2	Possible Assessment Activity 3
	Education Activity	Instructional Activity			
Solve word problems.	The teacher will demonstrate how to extract the relevant information from a word problem, set up the number sentence, and solve the equation. The students will solve word problems.	The teacher will demonstrate how to extract the relevant information from a word problem, set up the number sentence, and solve the equation. The students will perform a variety of story problems related to real life situations (shopping, hours worked, etc.) that require 2-4 basic operations.	Given a word problem or number sentence and two possible answers, the student will select the correct response.	Given a word problem or number sentence and three possible answers, the student will select the correct response.	Given a word problem or number sentence, the student will solve the problem.

## Ratios, Proportions, and Percents (Standard D)

#### 6.11.18 Set up, evaluate, or solve common problems involving percent (e.g., sales tax, tip, interest, discount, markup, commission, compound interest).

Critical Function	Suggested General	Suggested Modified	Possible Assessment Activity 1	Possible Assessment Activity 2	Possible Assessment Activity 3
	Education Activity	Instructional Activity			
Solve problems involving	The teacher will remind	The teacher will give the	Given the word problem, a	Given the word problem, a student	Given the word problem, a
percent.	students that total cost of	students a calculator;	student buys a sweatshirt that	buys a sweatshirt that costs \$20.	student buys a sweatshirt that
	an item can be found by	explain how to change %	costs \$20. The tax is 6%; the	The tax is 6%; the student will	costs \$20. The tax is 6%; the
	multiplying by 100%	into decimal and multiply	student will choose the correct	choose the correct amount of tax	student will calculate the tax.
	plus the tax (6% tax	by a cost to find tax.	amount of tax when given a	when given a list of possible taxes.	
	would require us to	Next, the teacher will	choice of two.		
	multiply by 1.06; 7%,	show how to add tax to			
	1.07, etc). The students	cost to find total price.			
	will then find the total	The students will then			
	cost in one step using	add tax to cost of items,			
	calculators.	using calculators.			

# Units, Tools, Estimation, and Application (Standards A, B, and C)

7.11.01 Change from one unit to another within the same system of measurement, including calculations with mixed units (e.g., 3 ½ hours plus 4 hours and 20 minutes; 2½ feet minus 16 inches).

Critical Function	Suggested General Education Activity	Suggested Modified Instructional Activity	Possible Assessment Activity 1	Possible Assessment Activity 2	Possible Assessment Activity 3
Change from one unit to another within the same system of measurement.	The teacher will review basic measurement facts with students and how to add and subtract in measurement units. The students will practice computing total time worked from time cards.	Same as suggested General Education Activity with necessary supports.	Given two times (12:00 to 1:00), the student will determine the amount of time, in hours, that has elapsed.	Given different times (12:00 to 1:00; 12:30 to 1:00), the student will match cards identifying hour and <sup>1</sup> / <sub>2</sub> hour.	Given a story problem using increments of time, the student will determine total time. Example: A man worked: 2 hrs. on Mon. 2 <sup>1</sup> / <sub>2</sub> hours on Tues. 3 <sup>1</sup> / <sub>2</sub> hours on Wed. What is the total time he worked?

# Units, Tools, Estimation, and Application (Standards A, B, and C)

# 7.11.03 Determine and calculate to an indicated precision the length, width, height, perimeter/circumference, area, volume, surface area, angle measures, or sums of angle measures of common geometric figures or combinations of common geometric figures.

Critical Function	Suggested General Education Activity	Suggested Modified Instructional Activity	Possible Assessment Activity 1	Possible Assessment Activity 2	Possible Assessment Activity 3
Determine and calculate to an indicated precision the length, width, height, perimeter, circumference, area, volume, surface area, angle measures, or sums of angle measures on common geometric figures or combinations of common geometric figures.	The teacher will review the definitions and formulas for surface area and volume. The students will calculate the surface area and volume of a cereal box by measuring its dimensions (length, width, and height).	Same as suggested General Education Activity with necessary supports.	Given a surface to measure and two different measurements, the student will choose the correct measurement.	Given a square table, the student will measure a side to determine the size of the tablecloth needed.	Given rectangular tables with different dimensions, the student will measure the tables' lengths and widths to determine the size of the tablecloth needed for each table.

## **Representations, Patterns, and Expression (Standard A)**

# 8.11.04 Determine a specific term, a finite sum, or a rule that generates terms of a pattern.

Critical Function	Suggested General	Suggested Modified	Possible Assessment Activity 1	Possible Assessment Activity 2	Possible Assessment Activity 3
	Education Activity	Instructional Activity			
Continue patterns and	The teacher will model	The teacher will model and	Given a pattern with one blank	Given a pattern with two blanks	Given a pattern with three blanks
tell how the pattern was	and describe how to	describe how to determine a	and the rule, the student will	and the rule, the student will	and the rule, the student will
created.	determine a rule that	rule that generates the rules	determine the missing number.	determine the missing numbers.	determine the missing numbers.
	generates the rules of a	of a pattern. Given a			
	pattern. The students will	number pattern of five			
	use an equation to find	numbers with two missing			
	the next number in a	numbers, the students will			
	pattern.	determine a specific pattern			
		to fill in the blanks.			

# **Connections Using Tables, Graphs, and Symbols (Standard B)**

## 8.11.12 Create and connect representations that are tabular, graphic, numeric, and symbolic from a set of data.

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Critical Function	Suggested General	Suggested Modified	Possible Assessment Activity 1	Possible Assessment Activity 2	Possible Assessment Activity 3
	Education Activity	Instructional Activity			
Make connections	The teacher will	The teacher will	Given a floor plan showing	Given a floor plan (see activity 1)	Given a floor plan (like from the
between different	model and explain	model and explain	multiple same-size tables and the	and several charts, the student will	modified activity), the student will
forms of data.	how to use an	how to use an	same number of chairs at each	determine which chart matches the	complete a chart that represents
	equation to create a	equation to create a	table; the students will complete a	floor plan.	the floor plan.
	graph. The students	graph. Given a floor	chart (for each table there are six		
	will practice using	plan showing multiple	chairs) to connect the data from		
	an equation and	same-size tables and	the floor plan to the chart.		
	turning it into a	the same number of	The student will be given two		
	table of ordered	chairs at each table;	choices of charts and will		
	pairs. The students	the students will	determine which chart matches the		
	will then graph the	complete a chart (for	floor plan.		
	ordered pairs.	each table there are			
		six chairs) to connect			
		the data from the			
		floor plan to the chart.			
		The students will			
		graph the pairs from			
		the chart.			

# **Properties of Single Figures and Coordinate Geometry (Standard A)**

9.11.02 Identify and represent transformations (rotations, reflections, translations,	, dilations) of an object in the plane, and describe the effects of transformations on points in words
or coordinates.	

Critical Function	Suggested General	Suggested Modified	Possible Assessment Activity 1	Possible Assessment Activity 2	Possible Assessment Activity 3
	Education Activity	Instructional Activity			
Identify and represent	The teacher will use a	The teacher will have the	Given a sample of a reflection	Given multiple samples of	Given art materials, the student
transformations.	Geometer's Sketch pad	students draw an object on one	and something that is not a	reflections and non-reflections,	will create their own reflection.
	to show the students how	side of the paper using	reflection, the student will choose	the student will sort the samples	
	to tessellate. The students	charcoal on a piece of paper.	the reflection.	by reflection and non-reflection.	
	will use rotations,	The students will be asked to			
	reflections, and	fold the paper and rub to			
	translations.	transfer the reverse image onto			
		the other side of the paper and			
		discuss that this is a reflection.			

# Properties of Single Figures and Coordinate Geometry (Standard A)

## 9.11.06 Identify a three-dimensional object from different perspectives.

Critical Function	Suggested General	Suggested Modified	Possible Assessment Activity 1	Possible Assessment Activity 2	Possible Assessment Activity 3
	Education Activity	Instructional Activity			
Identify a three-	The teacher will model	The teacher will model how a	Given a circle top view and a	Given examples of the shapes of	Given three-dimensional
dimensional object from	how a three-dimensional	three-dimensional shape looks	choice of a can of soup or a box	top views and examples of	objects, the student will create
different perspectives.	shape looks different	different from all points of	of cereal, the student will indicate	corresponding three-dimensional	the top view.
	from all points of view.	view. Given a top view of	which three-dimensional object	objects, the student will match	
	The students will identify	several three-dimensional	matches the circle top view.	the object to the top view of the	
	a three-dimensional	objects, the students will pick		correct shape.	
	object from different	out certain items based on the			
	perspectives and draw it	view from the top of the			
	from top view, side view,	object. For example, a box of			
	and front view.	cereal, search for a rectangle.			

## **Properties of Single Figures and Coordinate Geometry (Standard A)**

## 9.11.07 Identify the relationship between two-dimensional patterns (e.g., nets) and related three-dimensional objects (e.g., cylinders, prisms, cones).

Critical Function	Suggested General	Suggested Modified	Possible Assessment Activity 1	Possible Assessment Activity 2	Possible Assessment Activity 3
	Education Activity	Instructional Activity			
Identify the relationship	The teacher will have	The teacher will have students	Given a flattened-out paper	Given a flattened box and a	Given a three-dimensional
between two-dimensional	the students take a box	take a flattened-out box and	grocery bag and an open standing	choice of an open standing bag	object, the student will
patterns and related three-	and demonstrate as	assemble the box showing the	grocery bag, the student will	and an open standing box, the	determine which two-
dimensional objects.	many nets as possible.	relationship between what it	determine whether or not these	student will select the item that	dimensional pattern, when
	The students will	looked like flat and what it	are the same.	matches the flattened box.	folded, will make the three-
	identify the relationship	looks like assembled. The			dimensional object.
	between patterns and	students will assemble the box.			
	objects.				

#### Data Analysis and Statistics (Standards A and B)

#### 10.11.01 Read, interpret, predict, interpolate, extrapolate and use information from a variety of graphs, charts, and tables.

Critical Function	Suggested General	Suggested Modified	Possible Assessment Activity 1	Possible Assessment Activity 2	Possible Assessment Activity 3
	Education Activity	Instructional Activity			
Read, interpret, predict,	The teacher will review	Same as suggested General	Given choices, the student will	Given a graph, the student will	Given a graph, the student will
interpolate, and use	how to interpret data	Education Activity with	answer "yes" and "no" questions	answer two questions about the	read and interpret information
information from a	from a graph. The	necessary supports.	pertaining to information on a	graph.	about the graph.
variety of graphs, charts,	students will be given a		graph.		
and tables.	graph and asked to				
	predict answers based on				
	the graph.				